

Unconventional rf photoresponse from a superconducting spiral resonator

Alexander P. Zhuravel,¹ Cihan Kurter,² Alexey V. Ustinov,³ and Steven M. Anlage^{2,3}

¹*B. Verkin Institute for Low Temperature Physics and Engineering, National Academy of Sciences of Ukraine, 61103 Kharkov, Ukraine*

²*Center for Nanophysics and Advanced Materials, Department of Physics, University of Maryland, College Park, Maryland 20742-4111, USA*

³*Physikalisches Institut and Deutsche Forschungsgemeinschaft-Center for Functional Nanostructures (DFG-CFN), Karlsruhe Institute of Technology, D-76128 Karlsruhe, Germany*

(Received 9 March 2012; published 30 April 2012)

Superconducting thin film resonators employing strip geometries show great promise in rf/microwave applications due to their low loss and compact nature. However, their functionality is limited by nonlinear effects at elevated rf/microwave powers. Here, we show that by using a planar spiral geometry carrying parallel currents in adjacent turns, this limitation can be minimized. We investigate the rf current distributions in spiral resonators implemented with Nb thin films via laser scanning microscopy. The rf current density profile along the width of the individual turns of the resonators reveals an unconventional trend: maximum current in the middle of the structure and decaying toward its edges. This unusual behavior is associated with the circular nature of the geometry and the cancellation of magnetic field between the turns, which is favorable for handling high powers since it allows the linear characteristics to persist at high rf current densities.

DOI: [10.1103/PhysRevB.85.134535](https://doi.org/10.1103/PhysRevB.85.134535)

PACS number(s): 74.81.-g, 74.62.Dh, 74.25.nn

I. INTRODUCTION

Superconducting thin film rf/microwave resonators play a prominent role in many applications including quantum computing,^{1,2} single photon detection,³ bifurcation amplifiers,⁴ along with the quest to develop novel devices^{5,6} and media such as metamaterials.⁷⁻⁹ However, superconductors show nonlinear response when driven strongly by rf signals/microwaves,¹⁰⁻¹³ that manifests itself with a significant dependence of the surface resistance and reactance on the input power,¹⁴⁻¹⁷ P_{rf} . It is important to find an effective way to keep the resonant characteristics linear for a long range of P_{rf} to maximize the power handling capability of the resonators and expand their range of applicability.

Many superconducting resonators generally employ planar geometries made up of finite-width thin strips to carry a longitudinal high frequency current. The magnetic fields generated by flowing currents along the strips have a common characteristic of being perpendicular to the edges of the strip. Such a field configuration poses a challenge to the superconductor. In order to remain in the Meissner state, the strip must generate strong diamagnetic shielding currents to screen the perpendicular magnetic field from its interior. This gives rise to a large current buildup at the edges of a superconducting film shaped into a strip-geometry resonator.^{18,19} Screening currents can approach or exceed the critical current at the edges leading to a local breakdown of superconductivity and the onset of nonlinear behavior.²⁰ Therefore, the microwave properties of superconducting resonators are strongly dependent on the geometry of the design.¹⁷

Apart from simple single strip lines, coplanar waveguides,^{19,21} hairpin,²² and meander-line resonators²³ are other planar designs based on strip geometries. Many of these designs include parallel conductors where the currents in neighboring strips flow in opposite directions [see Fig. 1(a)]. This causes the induced normal oriented magnetic fields to be enhanced between the strips, and in turn results in an accumulation of rf screening currents at the edges. Such an inhomogeneous rf current density, J_{rf} can create changes in

the superconducting properties of the film, therefore limiting the functionality of the superconducting resonator by leading to nonlinearity in its response even at low stimulus.

Here we consider a unique resonator in the form of a continuous planar spiral designed to generate a strong electromagnetic response below 100 MHz. The spirals are intended to be deep subwavelength meta-atoms of a metamaterial, which could be utilized, for example, in magnetic resonance imaging applications as compact and low-loss flux guides.^{24,25} The resonators have a superior geometry in which the currents flowing in neighboring strips are in the same direction and approximately equal in magnitude, at least for the first few resonant modes [see Fig. 1(b)]. The perpendicular components of the induced magnetic fields largely cancel in the region between the windings, leading to a magnetic field pattern mainly parallel to the plane of the strips. This renders the distribution of total current density to be relatively uniform within the sample compared to the antiparallel current case discussed above, eliminating rf current buildup at the edges of the windings. This kind of configuration maintains the linear characteristics at elevated excitation power, and can be a better candidate in applications requiring linear rf/microwave response.

We have applied the spatially resolved technique of low-temperature laser scanning microscopy (LSM) to map rf current distributions globally (on the entire sample) and locally (in an individual winding) on spiral resonators made of Nb thin films. From the two-dimensional (2D) LSM images of the spirals excited at the fundamental resonance we have observed an unconventional rf current pattern with the absence of a buildup at the edges of the turns until a critical power value is reached. The evolution of the rf current distribution with increasing P_{rf} has been examined to investigate the power handling capability of these resonators.

The LSM technique has various contrast modes for imaging.²⁶ Here, we have utilized only two of them: optical reflectivity and ordinary high-frequency photoresponse modes. As was demonstrated in previous works,^{19,20} the response of the ordinary high-frequency photoresponse mode is a

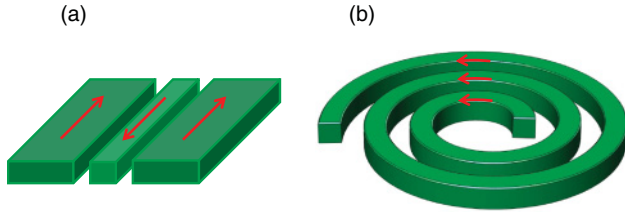


FIG. 1. (Color online) Schematic sketch of a coplanar wave guide (a) and a spiral resonator (b). The rf currents flow as shown with the red arrows when the resonators are excited.

superposition of two components; inductive and dissipative/resistive responses. Both generally require the superconducting sample to show a nonlinear response under laser irradiation. At low P_{rf} values, only laser heating plays a significant role in the nonlinearity, however once the power is elevated, extra dissipation mechanisms will be added due to rf heating. Such a response in superconductors well below their critical temperature T_c is mainly attributed to the formation of local dissipative (nonsuperconducting) domains where J_{rf} may exceed the local critical current density, J_c . The superconducting state is extremely sensitive to variations in the superfluid density that changes either with temperature or magnetic field, hence nonlinearity is inevitable.¹⁷ The effect manifests itself globally as distortion and/or bistable switching in the resonant transmission as a function of frequency, $|S_{21}(f)|$, at some microwave powers^{12,13,17,27} due to increased absorption of microwave radiation by quasiparticles.

II. SAMPLE

The LSM measurements presented in this paper use planar spiral resonators fabricated with 200-nm Nb thin films sputtered onto 350- μm thick single-crystal quartz substrates. Photolithography and reactive ion etching ($\text{CF}_4 : \text{O}_2$, 90% : 10%) are applied to give a spiral shape to the thin film. The T_c of the Nb film (9.2 K) is obtained from resistance vs temperature measurements.²⁵ Below the T_c of Nb, the microwave surface resistance, R_s of the film will be very small (about 20 $\mu\Omega$ at 10 GHz and 4 K).²⁸

Each spiral is made up of 40 turns, has an outer diameter of 6 mm and an inner diameter of 4.4 mm. The windings in the spirals and the spacing between them are of 10- μm width. Prior results show that the spirals act as very compact self-resonant strips, supporting up to ten half-wavelength standing waves of current along their length.²⁵

III. rf EXCITATION

A single spiral resonator is placed on a sapphire disk plate (50 mm in diameter, 2 mm in thickness) where a thermometer is attached nearby, in a cryogenic environment. The sample is stimulated with rf power applied via two coaxial cables terminated by shorted loops at the end with a diameter slightly larger than the outer diameter of the spiral as shown in Fig. 2. The planes containing the excitation (rf in) and the pickup loops (rf out) are parallel and the two loops are placed sandwiching the sample between them.⁷ The sample temperature is controlled with a heater located on the Cu cylinder on the cold head

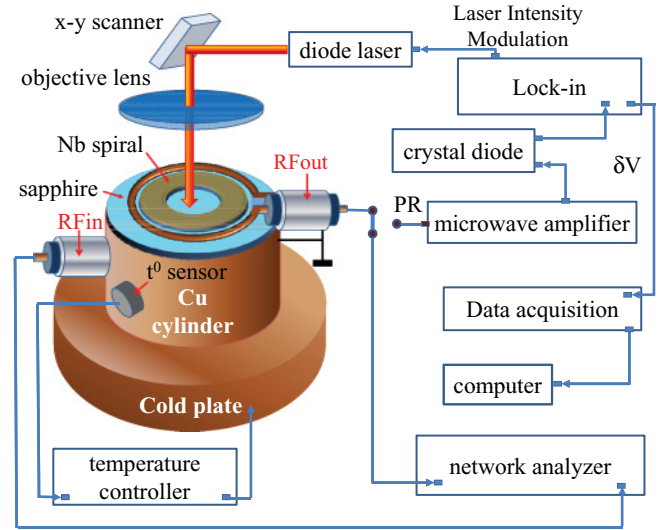


FIG. 2. (Color online) Simplified schematic representation of the LSM setup used for 2D visualization of microwave photoresponse of the tested resonator structure. Drawing is not to scale.

supporting the sapphire plate. The global resonant response was characterized with transmission measurements at different rf power levels between $P_{\text{rf}} = -30$ dBm and $+30$ dBm and at a bath temperature of $T_B = 4.5$ K using a microwave vector network analyzer (Anritsu MS4640A). From these measurements, the fundamental resonant frequency is found to be ~ 74 MHz, followed by higher harmonics.

IV. CRYOGENICS

Cooling the spiral samples in the range $T_c \geq T_B \geq 4.5$ K takes place inside the vacuum cavity of a variable temperature optical cryostat. The temperature of the cold Cu cylinder below the sample (50 mm in outer diameter with a 5-mm thick wall) (see Fig. 2) is stabilized with an accuracy of 1 mK. The cylinder temperature is controlled with a bifilar coil heater connected to the temperature controller and wound around the cold Cu plate having the same temperature as the cylinder. This Cu cylinder also cools both coaxial cables to eliminate a possible temperature gradient with the sample. The top surface of the sample faces the laser probe while the bottom surface is temperature stabilized by gluing it to the sapphire disk with cryogenic vacuum grease, assuring a reliable thermal heat sink. The same grease is used on the thermally conducting interface between the sapphire and Cu cylinder.

V. LASER SCANNING MICROSCOPY

For LSM imaging, the spirals are excited by rf signals, (while being kept well below the T_c of Nb) and illuminated by a focused laser beam acting as a noncontact optical probe. The LSM photoresponse (PR) dominantly comes from thermally induced changes in the rf transmission characteristics of the spiral due to absorption of the laser light with a wavelength of 670 nm. The smallest diameter of the laser probe spot is 1.5 μm when a 20 $\times$ magnification ($\text{NA} = 0.42$) objective lens is used for detailed LSM imaging (scan area up to $250 \times 250 \mu\text{m}^2$). Large-scale (up to an area of $50 \times 50 \text{ mm}^2$) LSM images

are acquired with an f -theta objective lens creating a 20- μm diameter laser illuminated spot. The intensity of the laser is modulated at a frequency of 100 kHz creating an oscillating thermal and/or optical probe. Changes in $|S_{21}(f)|$ due to the laser heating are synchronously detected with a lock-in amplifier.

In the bolometric (thermal) regime, the $\text{PR} \sim (\partial|S_{21}(f)|/\partial T)\delta T$ due to local temperature change δT , can be uniquely decomposed into inductive and resistive components.¹⁹ The inductive photoresponse, PR_I is proportional to $A\lambda^2(x,y)J_{\text{rf}}^2(x,y)\delta\lambda$, where A is the area heated by the laser spot and $\lambda(x,y)$ is the local value of the penetration depth at position (x,y) and can be interpreted as arising from the changes in penetration depth, $\delta\lambda$ induced by the laser heating. When $\lambda(x,y)$ and $\delta\lambda$ have uniform values, the PR_I has a profile proportional to the local value of rf current density squared, $J_{\text{rf}}^2(x,y)$. The resistive photoresponse, PR_R arises from thermally caused changes in the local resistance of the sample R_s and is a convolution of the laser modulated surface resistance, δR_s weighted by the local value of $J_{\text{rf}}^2(x,y)$.

In nonequilibrium (nonthermal) mode, the main mechanism of the LSM PR contrast is the following. Below T_c , the absorbed portion of laser power, δP_L causes nonequilibrium changes in the quasiparticle population, N_{QP} , resulting from the high-energy excitation of the superconducting film by individual optical photons with an energy of $hf_L = 1.85 \text{ eV} \gg 2\Delta_{\text{Nb}}(0)$ where Δ_{Nb} is the superconducting energy gap of Nb, h is Planck's constant, and f_L is the laser (irradiation) frequency. Because of electron-electron and electron-phonon scattering as well as direct Stokes-like depairing (with continuous frequency spectrum $hf \leq hf_L - 2\Delta_{\text{Nb}}$), every high-energy quasiparticle is capable of producing an extra population of low-energy excitations, $N_{\text{QP}} = \gamma hf_L / 2\Delta_{\text{Nb}}$, where γ is the quantum efficiency and smaller than 1. The excess quasiparticles create a nonequilibrium superconducting state due to the reduced superfluid density beneath the laser probe. As a result, local changes in $N_{\text{QP}}(\rho, \delta P_L)$ cause modifications in the surface impedance $\delta Z_s(\rho, \delta P_L) = \delta R_s(\rho, \delta P_L) + i\omega\delta L_k(\rho, \delta P_L)$ due to δR_s as well as photoinduced changes in local kinetic inductance, δL_k . Here, $\rho = \sqrt{(x - x_0)^2 + (y - y_0)^2}$ is the radial coordinate on the sample surface relative to the position (x_0, y_0) of the laser probe focus.

We observe that the Nb samples do not show any significant inductive photoresponse, PR_I at temperatures well below T_c . While increasing both rf and/or laser power, it has been found that resistive photoresponse, PR_R is produced at a lower critical rf power, P_{c1} corresponding to the first local switching of the sample into the nonlinear regime. The first detectable resistive component of PR can be written as

$$\text{PR}_R \propto |S_{21}(f, P_{\text{rf}})|^2 - |S_{21}(f, P_{\text{rf}} + \delta P_L)|^2 \quad (1)$$

for a condition of $J_{\text{rf}} \geq J_c(x_0, y_0, P_{\text{rf}}) - \delta J_c(x_0, y_0, P_L)$ combining the effects of the local microwave field (first term) and suppression of the critical current by the laser beam (second term).

It has been shown in the literature (see, for instance, Refs. 17 and 29) that the first nonlinear distortion of $|S_{21}(f)|$ appears as a deviation where the $|S_{21}(f)|$ curves fall on to curves with smaller quality factor, Q , in a narrow-band near

the resonant frequency f_0 (with P_{rf} exceeding P_{c1}). In the case of a small optical probe perturbation $\delta P_L \ll P_{c1} - \delta P_L$, the resistive component of LSM PR may be undetectable outside this narrow band, while strong PR signals are generated inside the band.

The LSM work presented here follows a modified procedure originally developed in Ref. 20, which is based on the insertion loss component of the photoresponse, PR_{IL} , rather than PR_I and PR_R measured at a frequency in the vicinity of f_0 . At a fixed rf frequency and spatially independent laser probe perturbation, the LSM PR is proportional to the laser-beam-induced changes in resonator transmission, $\delta|S_{21}(f)|^2$ that can be expressed in a form close to that introduced in Ref. 30.

$$\begin{aligned} \text{PR} &\propto \delta|S_{21}(f)|^2 \\ &= \frac{1}{2} \left(\frac{\partial|S_{21}(f)|^2}{\partial f_0} \frac{\partial f_0}{\partial P_L} + \frac{\partial|S_{21}(f)|^2}{\partial(1/2Q)} \frac{\partial(1/2Q)}{\partial P_L} \right. \\ &\quad \left. + \frac{\partial|S_{21}(f)|^2}{\partial\hat{S}_{21}^2} \frac{\partial\hat{S}_{21}^2}{\partial P_L} \right) \delta P_L \end{aligned} \quad (2)$$

where the transmission coefficient, $|S_{21}(f)|^2$ [ratio of the transmitted power, $P_{\text{rf}}^{\text{OUT}}(f)$, to the input power, $P_{\text{rf}}(f)$] as a function of driving frequency $f \sim f_0$ is given in the limit of weak coupling by³¹

$$|S_{21}(f)|^2 = \frac{\hat{S}_{21}^2}{1 + 4Q^2(f/f_0 - 1)^2} \quad (3)$$

and $\hat{S}_{21}^2$ is the maximum of the transmission coefficient at the peak of the resonance. By substitution of Eq. (3) in Eq. (2), one finds that the inductive

$$\text{PR}_I \propto \frac{\partial|S_{21}(f)|^2}{\partial f_0} = \frac{8\hat{S}_{21}^2 Q^2 (\frac{f}{f_0} - 1)}{[1 + 4Q^2 (\frac{f}{f_0} - 1)^2]^2} \frac{f}{f_0^2} \quad (4)$$

and the resistive

$$\text{PR}_R \propto \frac{\partial|S_{21}(f)|^2}{\partial(1/2Q)} = \frac{16\hat{S}_{21}^2 Q^3 (\frac{f}{f_0} - 1)^2}{[1 + 4Q^2 (\frac{f}{f_0} - 1)^2]^2} \quad (5)$$

components of total LSM PR are nulled at $f = f_0$, while the insertion loss component

$$\text{PR}_{\text{IL}} \propto \frac{|S_{21}(f)|^2}{\delta(\hat{S}_{21}^2)} = \frac{2\hat{S}_{21}^2}{1 + 4Q^2 (\frac{f}{f_0} - 1)^2} \quad (6)$$

is peaked at $f = f_0$.

In terms of local photo induced changes, PR_{IL} is directly linked with Ohmic dissipation generated by the laser probe at position (x_0, y_0) ,^{32,33}

$$\text{PR}_{\text{IL}}(x_0, y_0) \propto J_{\text{rf}}^2(x_0, y_0) \delta R_s(x_0, y_0). \quad (7)$$

In the frame of the paradigm described in Ref. 20 (in the case of a linear response function and a small probe perturbation) for a strip geometry oriented along the path L in the ℓ direction, the change in surface resistance due to a change in local critical current $[J_{\text{rf}} \geq J_c(\ell_0, P_{\text{rf}}) - \delta J_c(\ell_0, P_L)]$ at a specific

laser probe position ℓ_0 may be described as

$$\delta R_s(\ell_0) \propto \frac{\pi}{4} \frac{\Lambda}{WL} \int_{\mathcal{L}} d\ell \left. \frac{\partial R_s(\ell_0)}{\partial J_c(\ell_0)} \right|_{J=J_{rf}} \times \left. \frac{\partial J_c(\ell_0)}{\partial P_L} \right|_{P=P_{rf}^{CIRC}+\delta P_L} \delta P_L(\ell_0) \quad (8)$$

for large-scale imaging mode ($\Lambda \geq W$) where $\mathcal{L}$ is the path along the entire spiral with total length of L , W is the width of the film, P_{rf}^{CIRC} is the circulating rf power in the resonator and Λ is the characteristic healing length describing spatial decay of $PR_{IL}(\ell_0) \propto e^{-|\ell-\ell_0|/\Lambda}$ at a distance ℓ outside the intense beam focus.

As was postulated in Ref. 34, one can assume that both quantities $\partial R_s(x_0)/\partial J_c(x_0)$ and $\partial J_c(x_0)/\partial P_L$ are invariable in the probed sample area if d , δP_L , and Λ are spatially uniform through the whole resonator structure. Combining Eq. (7) with the integral value of Eq. (8) over the laser probe profile $\Lambda \delta P_L$ leads to

$$PR_{IL}(x_0) \propto \frac{1}{Wd} J_{rf}^2(x_0) \left. \frac{\partial R_s(x_0)}{\partial J_c(x_0)} \right|_{J=J_{rf}} \times \left. \frac{\partial J_c(x_0)}{\partial P_L} \right|_{P=P_{rf}^{CIRC}+\delta P_L} d\Lambda \delta P_L(x_0) \quad (9)$$

at location x_0 in the one-dimensional strip geometry.

Note that Eq. (9) demonstrates a threshold mechanism of PR_{IL} generation relative to excitations by both P_{rf}^{CIRC} and δP_L . In the undercritical state of the superconducting structure at $P = P_{rf}^{CIRC} + \delta P_L \leq P_{c1}$, the value of $\partial R_s(x_0)/\partial J_c(x_0)$ is zero at any position of the laser probe. In this case there is no $PR_{IL}(x_0)$ detectable by the LSM technique at f_0 in microwave imaging mode. In addition, very weak response is observed in purely normal regions of the sample. A detectable PR_{IL} signal is generated only in the narrow range of power between P_{c1} and P_{c2} (upper critical rf power). Note that P_{c1} [see Fig. 4(b)] denotes the total ($P_{rf}^{CIRC} + \delta P_L$) power initiating the first local dissipative source that destroys superconductivity. By P_{c2} we denote the power of this source giving rise to normal state switching. As seen from Eq. (9), $PR_{IL}(x_0)$ is proportional to $J_{rf}^2(x_0)$ in this range and spatial variations of LSM PR amplitude directly show the distribution of $J_{rf}^2(x_0)$ along that part of the standing wave that generates an overcritical state in the superconducting strips. Any deviation of $PR_{IL}(x_0)$ from the shape of a sinusoidal standing wave pattern then gives evidence for an inhomogeneous distribution of $J_c(x_0)$ due to the term $\partial J_c(x_0)/\partial P_L$ in Eq. (9). Also, it is clear that manipulations by both P_{rf} and δP_L may be used to probe local values of $J_c(x_0)$ as either P_{rf} or δP_L is increased.

In the case of 2D LSM probing (characteristic length of the laser-probe-induced nonequilibrium state, $\Lambda \leq$ strip width, W), the main LSM PR_{IL} imaging mode results from laser probe induced redistribution of the microwave current around the illuminated area. This effect leads to additional Ohmic dissipation in the nearby unilluminated areas of the superconducting strip generating

$$PR_{IL}(x_0, y_0) \propto \frac{\Lambda^2}{WL} \langle J_{rf}^2 \rangle_{W-W_c} \frac{\partial R_s(x_0, y_0)}{\partial J_c(x_0, y_0)} \frac{\partial J_c(x_0, y_0)}{\partial P_L} \delta P_L. \quad (10)$$

The effect is linked with the laser-induced modulation of the local critical current,

$$\delta I_c(x_0, y_0) = \frac{\pi \Lambda^2}{4} \frac{\partial J_c(x_0, y_0)}{\partial P_L} \delta P_L \quad (11)$$

underneath the laser probe allowing direct measurement of I_c . Here, $\partial J_c(x_0, y_0)/\partial P_L \propto J_c(x_0, y_0)$ if Λ and δP_L are independent of the beam position. Larger critical current densities produce larger LSM PR_{IL} as a result of redistribution of J_{rf} through the cross section of the undercritical currents of width $W - W_c$, thus increasing the averaged J_{rf} flowing there. Here W_c denotes the width of the critical region.

As one can see from Eq. (10), the highest microwave current densities produce the largest $PR_{IL}(x_0, y_0)$ resulting in quantitative profiles of $J_{rf}^2(x_0, y_0)$ in the area of the laser beam raster on the superconductor surface.

VI. GLOBAL PHOTORESPONSE RESULTS

To characterize the resilience of the superconducting spiral resonators at high P_{rf} , it is important to examine how current is distributed in the entire sample when driven by strong rf signals. Figure 3(a) is a 2D LSM image showing the global photoresponse of a Nb spiral excited at its fundamental resonant mode of 74 MHz. The laser is scanned over a $7.6 \times 7.6 \text{ mm}^2$ area at $T_B = 4.5 \text{ K}$, $P_{rf} = 14.8 \text{ dBm}$ and 1 mW laser power. The contrast in the image is mainly produced by PR_{IL} where the bright areas can be interpreted as $J_{rf}^2(x, y)$ to first approximation, and illustrates a mode in which a single half-wavelength of standing wave current spans the length of the spiral. As seen, rf current mainly flows in the middle windings in a quite uniform way, and diminishes toward the inner and outer edges of the spiral. Figure 3(b) is a 2D LSM

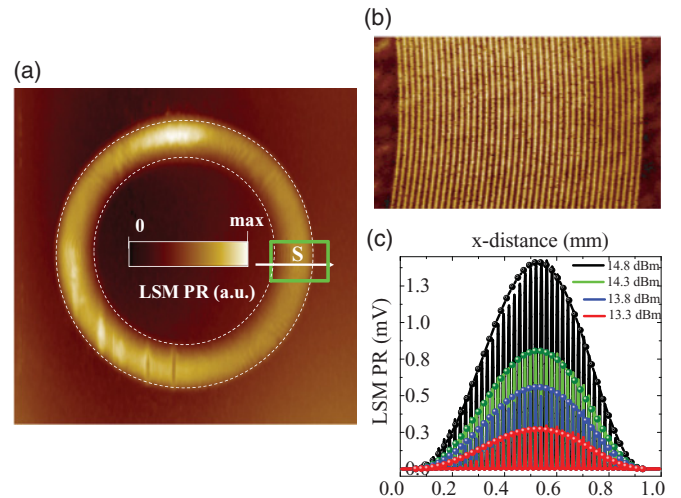


FIG. 3. (Color online) (a) 2D LSM image showing current distributions in a Nb spiral with an outer diameter of 6 mm and 40 turns, at the fundamental resonant mode of 74 MHz, $T_B = 4.5 \text{ K}$, $P_{rf} = 14.8 \text{ dBm}$. (b) 2D LSM reflectivity image showing the individual turns within an area on the spiral marked with a green box in (a). (c) The power-dependent PR_R along the cross section of the spiral shown with S line; maximum at the center, minimum at the edges. The dots are the estimated J_{rf}^2 profile for a simple standing wave current pattern at each P_{rf} .

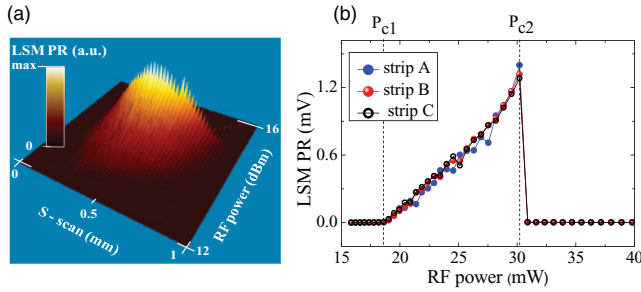


FIG. 4. (Color online) (a) 3D LSM image showing the power dependence of PR_{IL} over the S -line scan shown in Fig. 3(a). (b) Experimental LSM PR vs P_{rf} on a linear scale, taken at three neighboring strips (strip B is located at the center of the S -line scan between strip A and strip C). Both data are obtained at a temperature well below T_c , 4.5 K.

reflectivity image of the same spiral and shows the turns in an area on the spiral shown with the green box in Fig. 3(a).

The evolution of the PR_{IL} coming from the individual windings along the cross section of the spiral [marked as S in Fig. 3(a)] is shown in Fig. 3(c) for four different P_{rf} values and reveals the J_{rf} distribution in greater detail; note that the maximum PR corresponds to the center of the S cut line, and the ends show no response, confirming what is seen in Fig. 3(a). The asymmetric shape of the standing wave profile in the fundamental mode is understood from the fact that the spiral turns at larger radius have a greater circumference. The dots show the estimated J_{rf}^2 along the cut S for the case of a half sinusoid wave wrapped into a spiral. These dots describe well the observed PR_{IL} , indicating that the measured PR distribution is quite similar to the naive interpretation of imaging $J_{rf}^2(x, y)$.

In Fig. 4(a), the individual line scans of PR_{IL} at different incident power levels are shown in a three-dimensional (3D) image. Figure 4(b) shows power-dependent evolution of LSM PR at three fixed positions of the laser probe coinciding with the centers of three neighboring Nb strips (strips A, B, and C) exposed to maximum J_{rf} near the peak of the microwave standing wave. Note that a linear power scale is used. In the purely superconducting or normal states, LSM PR is not observable [notice the zero PR at the low and high limits of P_{rf} values in Fig. 4(a)]. As evident from Fig. 4(b), $PR_{IL}(S_{A,B,C}, P_{rf}) \propto J_{rf}^2(\sim P_{rf})$ shows an almost linear trend for a long range of nonequilibrium states of the Nb film starting from an P_{rf} corresponding to the first observable LSM PR at P_{c1} up to a switching to the normal state at $P_{c2} = 14.8$ dBm where the PR drops. These observations validate Eq. (9) in explaining our results. Also, one can see that based on the values of P_{c1} , the J_c of all three strips is practically the same, indicating a spatial uniformity in Nb film microstructure.

VII. LOCAL PHOTORESPONSE RESULTS

Upon more detailed examination of the Nb resonators, one can see that the LSM PR is also the strongest at the center of an individual turn forming the spiral, following the same trend of the global behavior shown in Fig. 3. Figure 5(a) shows 2D LSM PR_{IL} of a $40 \times 40 \mu\text{m}^2$ area on the same resonator scanned with a $1.5\text{-}\mu\text{m}$ diameter laser probe in the fundamental resonant mode of the spiral, a T_B of 4.5 K, and

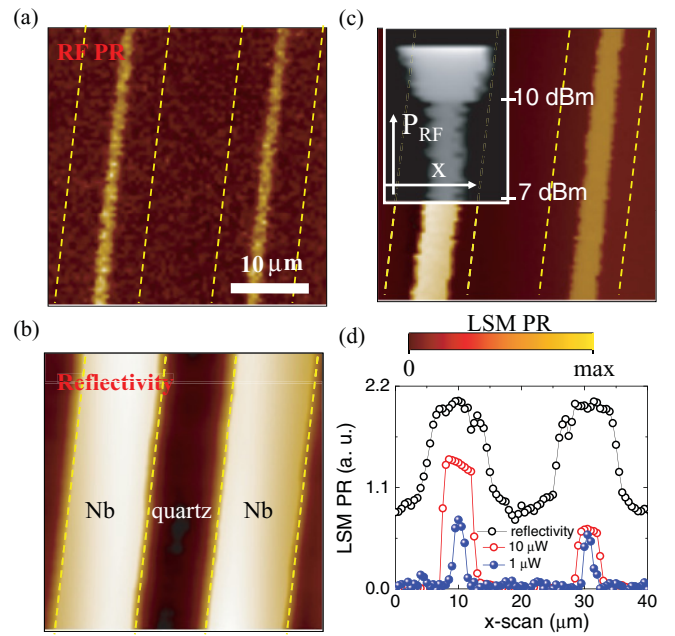


FIG. 5. (Color online) 2D LSM (a) PR_{IL} and (b) reflectivity images taken from $40 \times 40 \mu\text{m}^2$ area on the Nb spiral resonator at a laser power of about $1 \mu\text{W}$. (c) 2D LSM PR_{IL} image at $10 \mu\text{W}$. Inset shows rf power dependence of LSM PR_{IL} on the same area, showing the J_{rf} profiles at low and high rf stimulus. The x -line cut is at the same location in the figure and inset. (d) LSM PR coming from two neighboring Nb turns at two different laser powers; $1 \mu\text{W}$ and $10 \mu\text{W}$. The data are taken at $P_{rf} = 7$ dBm.

P_{rf} of 7 dBm, and laser power of $1 \mu\text{W}$, while Fig. 5(b) is a LSM reflectivity image obtained from the same area. By comparing the simultaneously measured LSM PR and reflectivity one finds that the PR is centered in the windings and does not extend to the edge of the strip. This observation is verified by studying the rf PR images as a function of increasing temperature or P_{rf} , and noting that the PR spreads out laterally in both directions from the center of the strip as the critical temperature and power are approached (see the power evolution of PR coming from Nb turns in Fig. 5(c); beyond +10 dBm the entire strip starts to show strong resistive response).

The accumulation of PR in the center of the turns is in contrast with previously published PR profiles of strip geometries that show substantial concentration of the LSM PR at the edges of current-carrying strips.^{26,33,35,36} Qualitatively, this fact can be easily understood. Here, the vertical components of magnetic field between the strips are partially canceled, as discussed above, since adjacent strips have nearly equal and parallel currents (at least in the fundamental mode). The spiral effectively acts like a disk carrying an approximately homogeneous current distribution, in which the current density goes to zero at the inner and outer radii of the disk.

As well as P_{rf} , laser power has an impact on the rf PR profile in the spirals. Figure 5(d) shows the initial depression of $J_c(x_0, y_0)$ by modulated laser power, $\delta P_L(x_0, y_0) = 1 \mu\text{W}$ in detail (blue curve). The main feature of $PR_{IL}(x_0, y_0)$ induced by δP_L is generated only inside a very narrow resistive strip, directed along the center of the strip line. Moreover, no

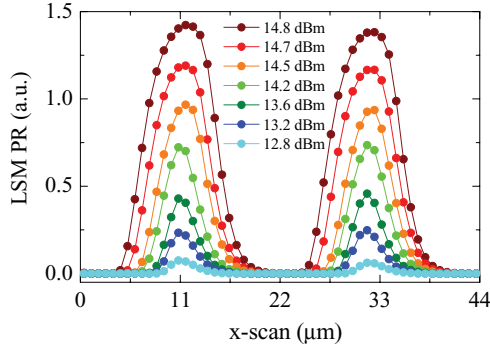


FIG. 6. (Color online) Power dependence of dissipative LSM PR_{IL} profiles showing the broadening of the critical state along the same $40\ \mu\text{m}$ line x scan through the width of two Nb turns at a laser power of about $1\ \mu\text{W}$.

spatial modulation in LSM PR is visible in the scanned area along the direction of rf current flow, indicating that the Nb film is quite homogenous, which rules out a structure-related mechanism of hot spot formation. Taking Eqs. (1) and (10) into account, as well as considering the fact that the laser beam illumination is spatially uniform, one can deduce that rf current is peaked half way between the Nb strip-line edges reaching local maxima of $J_{rf}(x_0, y_0) \leq J_c(x_0, y_0)$ there. Larger laser power [see the red curve in Fig. 5(d) corresponding to $\delta P_L(x_0, y_0) = 10\ \mu\text{W}$] increases the area of the strip in the critical state and consequently $J_{rf}(x_0, y_0)$ adjusts itself accordingly, since in the superconducting state, $J_{rf}(x_0, y_0)$ cannot exceed $J_c(x_0, y_0)$. Thus, the distribution of $PR_{IL}(x_0, y_0)$ spreads all over the strip occupying the dissipative regions of the still superconducting strip.

Line-scan profiles across two strips of such spatial evolution of $J_c(x)$ are shown in Fig. 6 as a function of P_{rf} . Small laser probe perturbation ($P_L = 1\ \mu\text{W} \ll P_{c1}$) generates the first observable LSM PR_{IL} exactly at the centers of the superconducting strips carrying a current density $J_{rf}(x_0, y_0) = J_c(x_0, y_0)$ at $P_{rf} = P_{c1} = 12.8\ \text{dBm}$, described by Eq. (10). Emergence of this signal is linked with the creation of submicron critical-state nonequilibrium domains at the centers of the strips, much smaller than the size of the laser probe. The full width half maximum (FWHM) of the position dependent LSM PR is about 2λ [see Figs. 5(d) and 6]. Further increase in P_{rf} leads to a broadening of the critical state area, which results in an increase of the FWHM of the dissipative LSM PR_{IL} profiles. With reference to Eq. (10) we see that as J_{rf} increases, the width of the film in the critical state (W_c) will increase, forcing more current into the undercritical region ($W - W_c$) and thus increasing $\langle J_{rf}^2 \rangle_{W-W_c}$.

Further, we estimate J_c by using the measured LSM PR_{IL} . In the inset of Fig. 5(c), there is a sharp transition from a center concentrated striplike resistive state to an almost uniform resistive state where PR covers the whole width of the strip. For a wide range of P_{rf} below $P_{c1} \sim 10\ \text{dBm}$, the LSM PR is almost independent of rf stimulus. We associate this effect with the auto-adjusting of instantaneous circulating J_{rf} to a value that could be accommodated in the superconducting resonator with varying local values of J_c . Considering the absence of visible imperfections in the reflectivity data taken from the same area

of this spatial power dependence we can confirm that this transition results from heating effects generated by hot spot formation at a location far from the scanned line. Thus, this defect-free section of the scan is chosen for rough estimation of the $J_c(x_0, y_0)$ limit for our resonator. Estimation is done based on measurements of P_{c1} generating the first detectable LSM resistive image similar to that shown in Fig. 5(a).

Since the use of smaller laser power is favorable in these measurements in terms of eliminating extra dissipation, we have scanned the spiral surface at $\delta P_L = 500\ \text{nW}$ and found that $P_{c1} \approx 9.5\ \text{dBm}$. There is no LSM PR observed below this laser power except only at very high P_{rf} . Using measured data [$P_{c1} = 8.91\ \text{mW}$ (9.5 dBm), $W = 10\ \mu\text{m}$, $d = 0.2\ \mu\text{m}$, $Q = 545.4$, $|S_{21}(f_0)| = 0.1553$, harmonic number $n = 3$, and $Z_0 = 96\ \Omega$, which is the characteristic impedance estimated for a coplanar waveguide of similar geometry] and a simple model for homogenous current distribution in the stripline we estimate an upper limit of J_c as³⁷

$$J_c(f_0) = \frac{1}{Wd} \sqrt{\frac{S_{21}(f_0)[1 - S_{21}(f_0)]4QP_{c1}}{n\pi Z_0}} \quad (12)$$

and obtain $J_c \sim 2.7 \times 10^{10}\ \text{A/m}^2$ from Eq. (12). This value is more than an order of magnitude smaller than the theoretical estimation for the depairing current density $J_{dp}^{GL}(T/T_c) \sim J_{dp}^{GL}(0)(1 - T/T_c)^{3/2}$, which is $0.44 \times 10^{12}\ \text{A/m}^2$ at 4.5 K [using $J_{dp}^{GL}(0) = 1.26 \times 10^{12}\ \text{A/m}^2$ for Nb at $T_B = 0\ \text{K}$].³⁸ This result implies that the measured critical current is limited by factors other than the depairing limit.

VIII. HIGHER HARMONICS

We observe that higher order harmonic modes of the Nb spiral resonator have more inhomogeneous current distributions in the windings due to the larger spatial gradients of the current. Moreover, the resonant characteristics of the Nb spiral are more power dependent in those higher modes than the fundamental mode.

Figures 7(a)–7(c) show LSM PR in the second to fourth harmonic standing wave patterns over a $7 \times 7\ \text{mm}^2$ area. If we focus on a small area ($125 \times 125\ \mu\text{m}^2$) in the third harmonic LSM image shown in Fig. 7(b), we see a different scenario from that discussed above [Fig. 7(d)]. In locations where there is a gradient in the current in the radial direction, a more traditional current profile is observed [notice the fourth turn from left in Fig. 7(d)]. Figure 7(e) shows the profile of this PR as a function of position in the radial direction. The PR is uniformly distributed across the strip at the peak of the standing wave pattern. However in regions where there is a significant change in the amount of current flowing in neighboring strips, the PR tends to be concentrated along one edge of the strip. For example on the right-hand side of Fig. 7(d) there are decreasing magnitudes of current flowing through the strips to the right. This leads to an asymmetry of the perpendicular magnetic field so that there is a larger field on the left side of each gap compared to the right. This in turn leads to an asymmetric buildup of current on the right side of each strip to screen out the field. The analogous phenomenon occurs on the other side of the peak in the current distribution as the current carried by windings further to the left decrease in magnitude.

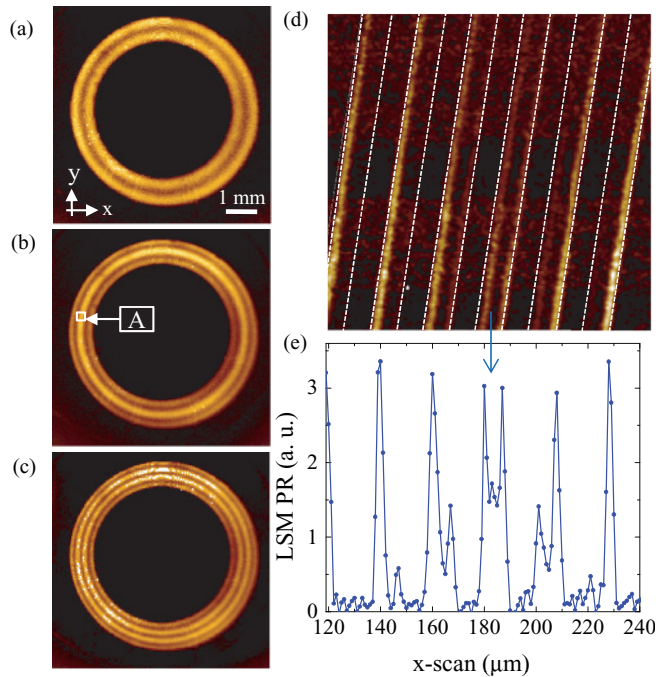


FIG. 7. (Color online) Large-scale $7 \times 7 \text{ mm}^2$ LSM PR images showing rf current induced dissipation in a Nb spiral at 4.5 K, 10 dBm and at (a) the second harmonic (219 MHz), (b) the third harmonic (355 MHz), and (c) the fourth harmonic (498 MHz). The area marked A in (b) indicates the position of a detailed 2D image (d) that shows the same rf dissipation in a $125 \times 125 \mu\text{m}^2$ region localized at the center of the $3\lambda/2$ standing wave pattern. (e) LSM PR profile along a $125\text{-}\mu\text{m}$ x scan corresponding to the bottom line-scan in (d).

We have seen similar effects in the third harmonic standing wave pattern of similar spirals implemented with $\text{YBa}_2\text{Cu}_3\text{O}_7$. Two distinct photoresponse peaks are seen on the edges of the $\text{YBa}_2\text{Cu}_3\text{O}_7$ strip. The maximum of the standing wave pattern

is visible in the middle strip, and the current decreases to either side.

IX. CONCLUSION

In conclusion, we have mapped the global and local current profile in planar spiral resonators implemented with superconducting Nb thin films via LSM imaging. The PR analyses reveal that the rf current in the fundamental mode mainly flows at the center of the turns of the spiral, which is contrary to the profile that is traditionally seen in strip-line and coplanar waveguide resonators. The continuous spiral geometry plays an important role in this unusual current profile contrasting with the conventional strip resonator case having antiparallel currents in adjacent elements where rf current accumulates at the edges.

ACKNOWLEDGMENTS

We gratefully acknowledge the contributions of John Abrahams, Tian Lan, Liza Sarytchev, Brian Straughn, and Frederic Sirois. The work at Maryland was supported by ONR Grants No. N000140811058 and No. 20101144225000, the US DOE DESC 0004950, the ONR/University of Maryland AppEl Center, Task D10 (N000140911190), and Center for Nanophysics and Advanced Materials (CNAM). The work in Karlsruhe is supported by the Fundamental Researches State Fund of Ukraine and the German Federal Ministry of Education and Research under Grant No. UKR08/011, the Deutsche Forschungsgemeinschaft (DFG) and the State of Baden-Württemberg through the DFG Center for Functional Nanostructures (CFN), and a National Academy of Sciences of Ukraine program on Nanostructures, Materials and Technologies. S.M.A. acknowledges sabbatical support from the CFN at Karlsruhe Institute of Technology.

¹R. J. Schoelkopf and S. M. Girvin, *Nature (London)* **451**, 664 (2008).

²R. C. Bialczak, M. Ansmann, M. Hofheinz, M. Lenander, E. Lucero, M. Neeley, A. D. O'Connell, D. Sank, H. Wang, M. Weides, J. Wenner, T. Yamamoto, A. N. Cleland, and J. M. Martinis, *Phys. Rev. Lett.* **106**, 060501 (2011).

³G. Goltsman, A. Korneev, A. Divoichiy, O. Minaeva, M. Tarkhov, N. Kaurova, V. Seleznev, B. Voronov, O. Okunev, A. Antipov, K. Smirnov, Yu. Vachtomin, I. Milostnaya, and G. Chulkova, *J. Mod. Opt.* **56**, 1670 (2009).

⁴M. B. Metcalfe, E. Boaknin, V. Manucharyan, R. Vijay, I. Siddiqi, C. Rigetti, L. Frunzio, R. J. Schoelkopf, and M. H. Devoret, *Phys. Rev. B* **76**, 174516 (2007).

⁵P. J. Burke, R. J. Schoelkopf, D. E. Prober, A. Sklare, W. R. McGrath, B. Bumble, and H. G. LeDuc, *Appl. Phys. Lett.* **68**, 3344 (1996).

⁶Benjamin A. Mazin, Daniel Sank, Sean McHugh, Erik A. Lucero, Andrew Merrill, Jiansong Gao, David Pappas, David Moore, and Jonas Zmuidzinas, *Appl. Phys. Lett.* **96**, 102504 (2010).

⁷Cihan Kurter, John Abrahams, and Steven M. Anlage, *Appl. Phys. Lett.* **96**, 253504 (2010).

⁸Cihan Kurter, Philippe Tassin, Lei Zhang, Thomas Koschny, Alexander P. Zhuravel, Alexey V. Ustinov, Steven M. Anlage, and Costas M. Soukoulis, *Phys. Rev. Lett.* **107**, 043901 (2011).

⁹S. M. Anlage, *J. Opt.* **13**, 024001 (2011).

¹⁰T. B. Samoilova, *Supercond. Sci. Technol.* **8**, 259 (1995).

¹¹M. Hein, *High-temperature-superconductor Thin Films at Microwave Frequencies* (Springer-Verlag, Berlin, 1999).

¹²G. Ghigo, R. Gerbaldo, L. Gozzelino, F. Laviano, and E. Mezzetti, *Phys. Rev. B* **82**, 054520 (2010).

¹³J. Ku, V. Manucharyan, and A. Bezryadin, *Phys. Rev. B* **82**, 134518 (2010).

¹⁴C. C. Chin, D. E. Oates, G. Dresselhaus, and M. S. Dresselhaus, *Phys. Rev. B* **45**, 4788 (1992).

¹⁵D. E. Oates, S. H. Park, and G. Koren, *Phys. Rev. Lett.* **93**, 197001 (2004).

¹⁶J. Wosik, L.-M. Xie, R. Grabovickic, T. Hogan, and S. A. Long, *IEEE Trans. Appl. Supercond.* **9**, 2456 (1999).

- ¹⁷C. Kurter, A. P. Zhuravel, A. V. Ustinov, and S. M. Anlage, *Phys. Rev. B* **84**, 104515 (2011).
- ¹⁸M. Ricci, H. Xu, R. Prozorov, A. P. Zhuravel, A. V. Ustinov, and S. M. Anlage, *IEEE Trans. Appl. Supercond.* **17**, 918 (2007).
- ¹⁹A. P. Zhuravel, S. M. Anlage, and A. V. Ustinov, *Appl. Phys. Lett.* **88**, 212503 (2006).
- ²⁰A. P. Zhuravel, S. M. Anlage, and A. V. Ustinov, *IEEE Trans. Appl. Supercond.* **17**, 902 (2007).
- ²¹G. Ghigo, R. Gerbaldo, L. Gozzelino, F. Laviano, G. Lopardo, E. Monticone, C. Portesi, and E. Mezzetti, *Appl. Phys. Lett.* **94**, 052505 (2009).
- ²²B. A. Willemsen, T. Dahm, and D. J. Scalapino, *Appl. Phys. Lett.* **71**, 3898 (1997); T. Dahm and D. J. Scalapino, *J. Appl. Phys.* **82**, 464 (1997).
- ²³A. P. Zhuravel, S. M. Anlage, S. K. Remillard, A. V. Lukashenko, and A. V. Ustinov, *J. Appl. Phys.* **108**, 033920 (2010).
- ²⁴M. C. K. Wiltshire, J. B. Pendry, I. R. Young, D. J. Larkman, D. J. Gilderdale, and J. V. Hajnal, *Science* **291**, 849 (2001).
- ²⁵C. Kurter, A. P. Zhuravel, J. Abrahams, C. L. Bennett, A. V. Ustinov, and S. M. Anlage, *IEEE Trans. Appl. Supercond.* **21**, 709 (2011).
- ²⁶A. P. Zhuravel, A. G. Sivakov, O. G. Turutanov, A. N. Omelyanchouk, S. M. Anlage, A. Lukashenko, A. V. Ustinov, and D. Abraimov, *Low Temp. Phys.* **32**, 592 (2006).
- ²⁷Matthew W. Brenner, Sarang Gopalakrishnan, Jaseung Ku, Timothy J. McArdle, James N. Eckstein, Nayana Shah, Paul M. Goldbart, and Alexey Bezryadin, *Phys. Rev. B* **83**, 184503 (2011).
- ²⁸M. S. Pambianchi, S. M. Anlage, E. S. Hellman, J. E. H. Hartford, M. Bruns, and S. Y. Lee, *Appl. Phys. Lett.* **64**, 244 (1994); M. S. Pambianchi, L. Chen, and S. M. Anlage, *Phys. Rev. B* **54**, 3508 (1996).
- ²⁹A. A. Zharov and A. N. Reznik, *Tech. Phys.* **43**, 117 (1998).
- ³⁰A. P. Zhuravel, S. M. Anlage, S. Remillard, and A. V. Ustinov, *Proceedings of the Sixth International Symposium on Physics and Engineering of Microwaves, Millimeter and Sub-millimeter Waves* (IEEE, 2007), Vol. 1, pp. 404–406.
- ³¹P. J. Petersan and S. M. Anlage, *J. Appl. Phys.* **84**, 3392 (1998).
- ³²A. P. Zhuravel, S. M. Anlage, and A. V. Ustinov, *Proceedings of the Seventh International Symposium on Physics and Engineering of Microwaves, Millimeter and Sub-millimeter Waves* (IEEE, 2010), Vol. 1, pp. 1–3.
- ³³J. C. Culbertson, H. S. Newman, and C. Wilker, *J. Appl. Phys.* **84**, 2768 (1998).
- ³⁴R. Gross and D. Koelle, *Rep. Prog. Phys.* **57**, 651 (1994).
- ³⁵A. P. Zhuravel, A. V. Ustinov, K. S. Harshavardhan, and S. M. Anlage, *Appl. Phys. Lett.* **81**, 4979 (2002).
- ³⁶A. P. Zhuravel, S. M. Anlage, and A. V. Ustinov, *J. Supercond. Nov. Magn.* **19**, 625 (2006).
- ³⁷D. E. Oates, A. C. Anderson, and P. M. Mankiewich, *J. Supercond.* **3**, 251 (1990).
- ³⁸A. Yu. Rusanov, M. B. S. Hesselberth, and J. Aarts, *Phys. Rev. B* **70**, 024510 (2004).